# Final Exam, SØK2010 Banking <br> Fall 2023 

Please answer your answers clearly and show your steps to receive partial credit. Final answers without discussions will not receive credit.

## Question 1 (25 points)

1. What problems does "asymmetry of information" create in the loan market? Can banks help to reduce the impact of this problem?
2. What is the difference between a bank that is insolvent and one that is illiquid?
3. What is the link between the safety net provided by the government to the banking system and the relatively heavy regulation of the same industry by the government?

## Question 2 (25 points)

Consider a two-period economy, in which the agent has preference described by $u\left(c_{1}, c_{2}\right)=$ $\log c_{1}+0.9 \log c_{2}$, where $c_{1}$ and $c_{2}$ are consumption in the each period respectively. $u$ is strictly increasing and concave. The agent has income $y_{1}=2$ in the first period and $y_{2}=1$ in the second. Assume there is no transaction cost in the financial market, and the agent optimizes his utility through borrowing or lending in the first period, and repaying or getting paid back at the gross interest rate of $r=1.25$ in the second period.

1. Write down the optimization problem of the agent. Solve the optimal borrowing or lending decision.
2. Solve the agent's optimal consumption in both periods.
3. Is the agent better off with the financial market compared to without the financial market? Explain.
4. Now assume that the financial market is not perfect, and the borrowing rate $r_{b}=$ 1.25 is bigger than the saving rate $r_{s}=1.15$. What is the agent's optimal behavior now: will he borrow or lend?
5. Show that transaction costs reduce the utility of the agent.

## Question 3 (25 points)

Let's take a closer look at the simple model of "liquidity insurance" presented in "Banks and Liquidity Creation: A Simple Exposition of the Diamond-Dybvig Model" and sketched in class. Following Diamond, let's use the utility function $u(c)=1-\frac{1}{c}$, and let's assume the probability of a consumer having to withdraw her money after only one period is $\frac{1}{4}$, with probability $\frac{3}{4}$ she can leave the funds in the investment for the full two periods. She earns a return of 1 if the funds are withdrawn after one period, and 2 if they are invested for two periods.

1. Find consumers' expected utility in the scenario where they enjoy $u(1)$ with probability $\frac{1}{4}$ and $u(2)$ with probability $\frac{3}{4}$.
2. Now assume an intermediary, call it a "bank", pays depositors the same amount of money regardless of whether the funds are left for one or two periods (this assumption is a little strange, but it makes things simple). Determine the amount the bank has to pay in order to make the consumers just as well off as they would have been in part (1).
3. Find the bank's expected profits if it pays the amount determined in part (2), and determine the maximum share of depositors that could demand their money after one period without making the bank insolvent.
4. Now suppose increased competition forces the bank to pay 1.7 to depositors, instead of what you got in (2). Find the bank's profits, and the maximum share of "early withdrawals" the bank could sustain without becoming insolvent.
5. Do you think it's reasonable to assume that depositors' liquidity demands are independent-that is, that the probability of any given depositor coming in for her funds does not depend on whether other depositors are coming in for their funds? Explain. Intuitively, what effect would the failure of this assumption have on the probability of insolvency?

## Question 4 (25 points)

| Assets |  |  | Liabilities and Equity |  |
| :--- | :--- | :--- | :--- | :---: |
| Cash and due from banks | 9000 | Demand deposits | 19000 |  |
| Investment securities | 23000 | Term deposits | 89000 |  |
| Repurchase agreements | 42000 | Retail CDs | 28000 |  |
| Loans | 90000 | Debentures | 19000 |  |
| Fixed assets | 15000 | Total liabilities | 155000 |  |
| Other assets | 4000 | Common stock | 12000 |  |
|  |  | Paid-in capital | 4000 |  |
|  |  | Retained earnings | 12000 |  |
| Total assets | 183000 | Total liabilities/equity | 183000 |  |

Income statement
Interest on loans ..... 9000
Interest on investment securities ..... 4000
Interest on REPOs ..... 6000
Interest on bank deposits ..... 1000
Total interest income ..... 20000
Interest on deposits ..... 9000
Interest on debentures ..... 2000
Total interest expense ..... 11000
Net interest income ..... 9000
Provision for loan losses ..... 2000
Noninterest income ..... 2000
Noninterest expenses ..... 1000
Income before taxes ..... 8000
Taxes ..... 3000
Net income ..... 5000

A bank's balance sheet and income statement are given. Based on the given information, calculate the quantities in 1)-4).

1. Return on equity
2. Return on assets
3. Equity multiplier
4. Net interest margin
